

**Mark Scheme 4734
January 2006**

STATISTICS 3

1	(i)	$p_s \pm Z\sigma_{est}$	M1	Use formula, σ involving p_s and
		400.		
		$p_s=186/400(0.465)$	A1	
		$\sigma_{est} = \sqrt{\frac{0.465 \times 0.535}{400}}$	B1	
		$z=1.96$	A1	
		(0.416, 0.514)	A1	5

(ii)	Councillor statement implies $p=0.5$. CI does contain 0.5 but only just so councillor probably correct.	B1	1	Any justifiable comment Not too assertive
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2	(i)	σ^2 unknown	B1	1
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(ii)	$H_0: \mu=2000$ (or \geq), $H_1: \mu < 2000$	B1		
	$\bar{x}=1958.2$, $s=115.57$	B1B1		or 1958, 115.6
	EITHER: Test statistic = $\frac{1958.2 - 2000}{115.57/2}$	M1		
	=-0.7234	A1		art -0.723
	Critical value -1.638	B1		
	Test statistic not in CR, accept H_0		M1	Or equivalent
	Accept that specification is being met	A1		Conclusion in context
OR:	Critical region:			
	$\frac{\bar{x} - 2000}{115.57/2} < t$	M1		
	$t=-1.638$		B1	
	$\bar{x} < 1905.2$	A1		art 1900 or 1910
	As above	M1A1	8	Conclusion in context

3	(i)	Use of $\int_{20}^a f(t)dt$	M1	With limits and $f(t)$ substituted
		$\left[-\frac{2}{3} \cos \frac{\pi t}{60} \right]_{20}^a$	A1	
		AG	A1	3
				Properly obtained

(ii)	$3 \times (i) + 2 \times (1-(i))$	M1		Idea of expectation
	Equate to 2.80 and attempt to solve	A1		All correct
	$a=44.8$		M1	From equation in a, 2 or 3
		A1	4	Accept 45
				SR: $\frac{1}{3}(1-2\cos..)= 0.8$ give max 3/4

4 (i) Use Poisson distribution M1 Po(5.5) or Po(55) seen
 With $\mu=55$ B1
 $\sigma^2=55$ A1
 $(39.5-55)/\sqrt{55}$ A1 Standardising, with ,without or
 -2.09 A1 wrong cc
 art 0.982 A1 **6**

(ii) $E(X- Y)=37$ B1√ ft μ above
 $Var(X- Y)=55+18$ M1
 $=73$ A1√ **3** ft μ above

(iii) EITHER: Expectation not equal to variance M1 Any one
 OR: $X-Y$ could be negative
 OR: Difference of two Poisson variables
 could have a negative expectation
 So $X-Y$ does not have a Poisson distn A1 **2**

5 (i) EITHER: Use $\frac{1}{8}(3-1)^2=a(3-2)$ M1 Continuity of F
 OR: $a(4-2)=1$ A1 **2**
 $a=\frac{1}{2}$

(ii) $F(1.8)=\frac{1}{8}(0.8)^2$ M1 Appropriate use of F
 $=0.08$
 $C_X(8)=1.8$ A1 **2**

(iii) $G(y)=P(Y \leq y)=P((X-1)^{1/2} \leq y)$ M1
 $=P(X \leq y^2+1)$ A1
 $=F(y^2+1)$ A1

$$G(y) = \begin{cases} \frac{1}{8}y^4 & (0 \leq y \leq \sqrt{2}), \\ \frac{1}{2}(y^2 - 1) & (\sqrt{2} < y \leq \sqrt{3}). \end{cases}$$
 A1

Ignore others, A1 for both ranges of y B1 **5**

(iv) Use $G(y)$ to find $C_Y(8)$ M1
 Obtain $\sqrt{0.8}$ A1
 Correct verification B1 **3**

6	(i)	$s^2=(8 \times 0.7400+9 \times 0.8160) / 17$	M1	2	Formula for pooled estimate At least 4DP shown
		$=0.7802$ 0.780 AG	A1		

6	(ii)	Assumes braking distances have normal distributions	B1	5	Must be t value Allow 0.780 art (1.52, 3.60)
		Use $\bar{x}_A - \bar{y}_B \pm t\sigma$	M1		
		$t=2.567$	A1		
		$\sigma=\sqrt{[0.7802(1/10+1/9)]}$ (0.40584)	B1		
		(1.518, 3.602)	A1		

6	(iii)	$H_0: \mu_A - \mu_B = 2, H_1: \mu_A - \mu_B > 2$	B1	6	For both hypotheses Standardising, σ as above Rounding to 1.38 2.70 or 2.71 Not from different signs test statistic critical value. A1 dep on correct H_0 and H_1
		Use of CV, 1.740	B1		
		EITHER: Test statistic $= (2.56 - 2) / \sigma$	M1		
		$= 1.38$	A1		
		OR: Critical region			
		$\bar{x}_A - \bar{x}_B > 2 + 1.74 \times 0.4054$	M1		
$= 2.7054$	A1				

7	(i)	Use $\int_1^\infty x\alpha x^{-\alpha-1} dx = \left(\int_1^\infty \alpha x^{-\alpha} dx\right)$	M1	3	Correct limits not required Properly obtained
		$\left[\frac{-\alpha x^{-\alpha+1}}{\alpha-1}\right]_1^\infty$ $= \alpha/(1-\alpha)$ AG	B1 A1		

7	(ii)	$\alpha(1-\alpha)=1.92$ giving 2.087 AG	B1	4	Evidence required
		(iii) Integral of $2.087x^{-3.087}$ from 2 to 3	M1		
		$[-x^{-2.807}]_2^3$	A1		
		$\times 200$ Obtain AG	A1 A1		

7	(iv)	Combine last 3 cells	B1	6	Accept one error All correct art 5.8 ft number of sells used.
		$X^2 = 6.9^2/152.9 + 6.1^2/26.9$	M1		
		$+ 4.9^2/9.1 + 4.1^2/11.18$	A1		
		$= 5.847\dots$	A1		
		Use CV 5.991	B1 $\sqrt{\quad}$		
		Accept that data supports Zipf's law	B1		
SR: From 6 cells: B0M1A1 (for 9.34) then B1 for 9.488, B1 Max 4/6					